

```

In[762]:= k = 2;
a = 0.5;
a1 =  $\frac{(a^2 - 1)}{2}$ ; (*0.1,0.5,1,3*)
a2 = (a^2 - 1) a1;
We = 0;
x[1] = 0;
H = .666667;
For[ii = 1, ii ≤ 11, ii++,
  h = k - (k - 1) * x[ii];
  sol = NDSolve[{D[(u'[y] + We^2 a1 (u'[y])^3 + We^4 a2 (u'[y])^5), y, y] == 0, u[0] == 0,
    u'[0] == 1, u[h] == H, u'[h] == 0}, {u[y], u'[y], u''[y], u'''[y]}, {y, 0, h}];
  ppx = Table[(u^(3)[y] + 3 a1 We^2 u''[y]^2 u^(3)[y] + 5 a2 We^4 u''[y]^4 u^(3)[y]) /. sol,
    {y, 0, h, 0.1}];
  px[ii] = (u^(3)[y] + 3 a1 We^2 u''[y]^2 u^(3)[y] + 5 a2 We^4 u''[y]^4 u^(3)[y]) /. sol /. y → 0;
  x[ii + 1] = x[ii] + 0.1;
];
tt = Table[{x[ii], px[ii][[1]]}, {ii, 1, 11}];
fff = Interpolation[tt];
ggg = Integrate[Interpolation[tt][x], x];
hhh = Integrate[ggg, {x, 0, 1}];
Table[ggg, {x, 1, 1}]
(*pressure*)
Plot[ggg, {x, 0, 1}, Frame → True,
  PlotStyle → {{Thin, Black}}, LabelStyle → Directive[Black, 12],
  FrameLabel → {"", "", " ", ""}, FrameStyle → Directive[Thin],
  LabelStyle → Directive[18], Epilog → {Arrow[{{}}, {}], Text[""]}]
(*pressure gradient*)
Plot[fff[x], {x, 0, 1}, Frame → True, PlotRange → All,
  PlotStyle → {{Thick, Black}}, LabelStyle → Directive[Black, 12],
  FrameLabel → {"", "", " dp/px ", ""}, FrameStyle → Directive[Thin],
  LabelStyle → Directive[18], Epilog → {Arrow[{{}}, {}], Text[""]}]
(*velocity*)
Plot[u'[y] /. sol, {y, 0, h}, Frame → True,
  PlotStyle → {{Thick, Black}}, LabelStyle → Directive[Black, 12],
  FrameLabel → {"", "", " v ", ""}, FrameStyle → Directive[Thin],
  LabelStyle → Directive[18], Epilog → {Arrow[{{}}, {}], Text[""]}];

```

Out[773]= {0.0000240367}

```

In[777]:= p111 = cer2[0., 0.];
0.0000240367 • Spacer2[0.];
0.

```

```

In[810]:= a = 0.5;
η = 1;

```

$$\mu = 1;$$

$$k = 2; (*0.2, 0.3*)$$

$$b = 0;$$

$$\alpha_1 = \frac{(a^2 - 1) \eta}{(\eta + \mu)}; (*0.1, 0.5, 1, 3*)$$

$$\alpha_2 = (a^2 - 1) \alpha_1;$$

$$pp = -\frac{6(-1+k)(-1+x)x}{(1+k)(k+x-kx)^2} -$$

$$\frac{1}{25k(1+k)^3(k+x-kx)^6} 12b^2(-1+k)(-1+x)x(k^3(79+k(-32+k(77+26k))) -$$

$$(-1+k)k^2(63+k(55+k(191+91k)))x + 3(-1+k)^2k(29+k(49+k(53+39k)))x^2 - (-1+k)^3(1+5k)(13+k(8+13k))x^3 + (-1+k)^4(13+k(8+13k))x^4) \alpha_1 +$$

$$\frac{1}{30625k^3(1+k)^5(k+x-kx)^{10}} 8b^4(-1+k)(-1+x)x$$

$$(9(-1+k)^2(26164k^{12}(-2+x)(-1+x)^7 + 26164x^7(1+x) + kx^6$$

$$(209312 + (26439 - 235201x)x) - k^{11}(-1+x)^6(-550 + x(-443963 + 235201x)) +$$

$$2k^{10}(-1+x)^5(-10945 + x(75985 + x(-906523 + 487927x))) +$$

$$2k^2x^5(353556 + x(-273280 + x(-557258 + 487927x))) + 4k^6(-1+x)x$$

$$(-168418 + (-1+x)x(-476296 + (-1+x)x(346861 + 1655413(-1+x)x))) -$$

$$5k^3x^4(-282331 + x(438137 + x(341729 + x(-1035337 + 498297x)))) -$$

$$5k^9(-1+x)^4(-39505 + x(-8772 + x(225500 + x(-957851 + 498297x)))) + 20k^4$$

$$x^3(85379 + x(-199689 + x(-23569 + x(560189 + 11x(-58191 + 20203x)))) +$$

$$20k^8(-1+x)^3(-4442 + x(-15499 + x(-38722 + x(222115 +$$

$$11x(-42824 + 20203x)))) + k^5x^2(1427274 + x(-4230511 + 2x$$

$$(872810 + x(6586595 + x(-13525745 + (10584551 - 3015409x)x)))) -$$

$$k^7(-1+x)^2(-202367 + x(234941 + 2x(-92500 + x(-1979055 +$$

$$x(5834125 + x(-7507903 + 3015409x)))))) \alpha_1^2 - 250(2k^7(3616 +$$

$$k(-4429 + k(4302 + k(-3193 + k(2038 + k(1683 + k(-1031 + 689k)))))) -$$

$$(-1+k)k^6(17267 + k(-21021 + k(15543 + k(-6983 +$$

$$k(14973 + k(25929 + k(-16843 + 10335k)))))) x +$$

$$(-1+k)^2k^5(40814 + k(-38829 + k(11524 + k(44317 + k(9938 +$$

$$k(88291 + k(-59476 + 33761k)))))) x^2 -$$

$$(-1+k)^3k^4(46410 + k(-31846 + k(-1865 + k(138739 + k(-36884 +$$

$$k(173044 + 13k(-9125 + 4823k)))))) x^3 +$$

$$(-1+k)^4k^3(40306 + k(-994 + k(-37264 + k(190331 + k(-92344 +$$

$$5k(42550 + k(-29230 + 14469k)))))) x^4 -$$

$$(-1+k)^5k^2(19292 + k(11438 + k(-58254 + k(155082 + k(-97575 +$$

$$k(167361 + k(-113837 + 53053k)))))) x^5 +$$

$$(-1+k)^6k(5512 + k(11044 + k(-38486 + k(78060 + k(-56266 +$$

$$k(81919 + k(-54688 + 24115k)))))) x^6 - (-1+k)^7(1+9k)$$

$$(689 + k(-1720 + k(2714 + k(-2228 + k(2714 + k(-1720 + 689k)))))) x^7 +$$

$$(-1+k)^8(689 + k(-1720 + k(2714 + k(-2228 + k(2714 + k(-1720 + 689k))))))$$

$$x^8) \alpha_2);$$

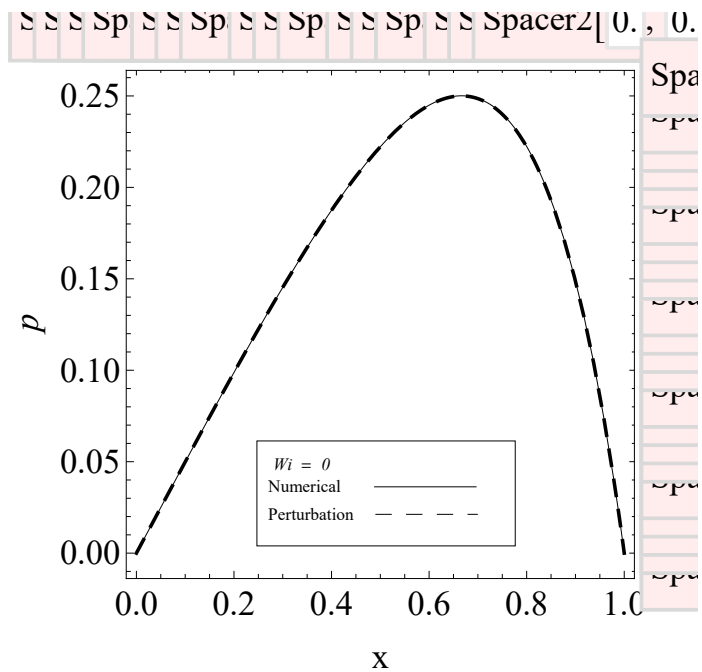
Plot[pp, {x, 0, 1}, PlotStyle -> {Thickness[0.007], Dashing[.030], Black},
LabelStyle -> Directive[Black, 12]]

$\ln[817]:= \mathbf{p1111} = \begin{matrix} 0.25 \\ 0.20 \\ 0.15 \\ 0.10 \end{matrix} \begin{matrix} \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \end{matrix} \begin{matrix} 0.2 \\ 0.4 \\ 0.6 \\ 0.8 \\ 1.0 \end{matrix} ;$

$\ln[794] := \mathbf{p} = \begin{matrix} 0.25 \\ 0.20 \\ 0.15 \\ 0.10 \end{matrix} ;$

`ln[778]:= p22 =`  ;

```
In[819]:= Show[{p111, p1111}, Frame → True, PlotRange → All, LabelStyle → Directive[Black, 18],
  AspectRatio → 1, FrameLabel → {"x", "p", " a = 0.5, k = 2", ""},
  FrameStyle → Directive[Thin], LabelStyle → Directive[Black, 18], Axes → False]
```



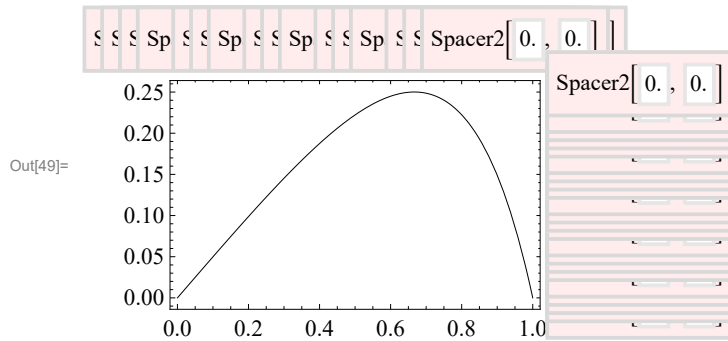
```

In[35]:= k = 2;
a = 0.5;
a1 =  $\frac{(a^2 - 1)}{2}$ ; (*0.1,0.5,1,3*)
a2 = (a^2 - 1) a1;
We = 0;
x[1] = 0;
H = .66667;
For[ii = 1, ii ≤ 11, ii++,
  h = k - (k - 1) * x[ii];
  sol = NDSolve[{D[(u'[y] + We^2 a1 (u'[y])^3 + We^4 a2 (u'[y])^5), y, y] == 0, u[0] == 0,
    u'[0] == 1, u[h] == H, u'[h] == 0}, {u[y], u'[y], u''[y], u'''[y]}, {y, 0, h}];
  ppx = Table[(u^(3)[y] + 3 a1 We^2 u''[y]^2 u^(3)[y] + 5 a2 We^4 u''[y]^4 u^(3)[y]) /. sol,
    {y, 0, h, 0.1}];
  px[ii] = (u^(3)[y] + 3 a1 We^2 u''[y]^2 u^(3)[y] + 5 a2 We^4 u''[y]^4 u^(3)[y]) /. sol /. y → 0;
  x[ii + 1] = x[ii] + 0.1;
];
tt = Table[{x[ii], px[ii][[1]]}, {ii, 1, 11}];
fff = Interpolation[tt];
ggg = Integrate[Interpolation[tt][x], x];
hhh = Integrate[ggg, {x, 0, 1}];
Integrate[ggg, {x, 0, 1}]
Table[ggg, {x, 1, 1}]
(*pressure*)
Plot[ggg, {x, 0, 1}, Frame → True,
  PlotStyle → {{Thin, Black}}, LabelStyle → Directive[Black, 12],
  FrameLabel → {"", "", " ", ""}, FrameStyle → Directive[Thin],
  LabelStyle → Directive[18], Epilog → {Arrow[{{}}, {}], Text[""]}]
(*pressure gradient*)
Plot[fff[x], {x, 0, 1}, Frame → True, PlotRange → All,
  PlotStyle → {{Thick, Black}}, LabelStyle → Directive[Black, 12],
  FrameLabel → {"", "", " dp/px ", ""}, FrameStyle → Directive[Thin],
  LabelStyle → Directive[18], Epilog → {Arrow[{{}}, {}], Text[""]}]
(*velocity*)
Plot[u'[y] /. sol, {y, 0, h}, Frame → True,
  PlotStyle → {{Thick, Black}}, LabelStyle → Directive[Black, 12],
  FrameLabel → {"", "", " v ", ""}, FrameStyle → Directive[Thin],
  LabelStyle → Directive[18], Epilog → {Arrow[{{}}, {}], Text[""]}]

```

Out[47]= 0.158941

Out[48]= {0.000010537}



In[10]:= $u1 = \frac{\text{erf}\left(\frac{x}{0.06}\right)}{0.1} \text{Spacer2}[0.];$

In[11]:= $a = 0.5;$

$\eta = 1;$

$\mu = 1;$

$k = 2; (*0.2, 0.3*)$

$b = 0.5;$

$\alpha_1 = \frac{(a^2 - 1) \eta}{(\eta + \mu)}; (*0.1, 0.5, 1, 3*)$

$\alpha_2 = (a^2 - 1) \alpha_1;$

$pp = -\frac{6(-1+k)(-1+x)x}{(1+k)(k+x-kx)^2} -$

$\frac{1}{25k(1+k)^3(k+x-kx)^6} 12b^2(-1+k)(-1+x)x(k^3(79+k(-32+k(77+26k))) -$

$(-1+k)k^2(63+k(55+k(191+91k)))x + 3(-1+k)^2k(29+k(49+k(53+39k)))x^2 - (-1+k)^3(1+5k)(13+k(8+13k))x^3 + (-1+k)^4(13+k(8+13k))x^4) \alpha_1 +$

$\frac{1}{30625k^3(1+k)^5(k+x-kx)^{10}} 8b^4(-1+k)(-1+x)x$

$(9(-1+k)^2(26164k^{12}(-2+x)(-1+x)^7 + 26164x^7(1+x) + kx^6$

$(209312 + (26439 - 235201x)x) - k^{11}(-1+x)^6(-550 + x(-443963 + 235201x)) +$

$2k^{10}(-1+x)^5(-10945 + x(75985 + x(-906523 + 487927x))) +$

$2k^2x^5(353556 + x(-273280 + x(-557258 + 487927x))) + 4k^6(-1+x)x$

$(-168418 + (-1+x)x(-476296 + (-1+x)x(346861 + 1655413(-1+x)x))) -$

$5k^3x^4(-282331 + x(438137 + x(341729 + x(-1035337 + 498297x)))) -$

$5k^9(-1+x)^4(-39505 + x(-8772 + x(225500 + x(-957851 + 498297x)))) + 20k^4$

$x^3(85379 + x(-199689 + x(-23569 + x(560189 + 11x(-58191 + 20203x)))) +$

$20k^8(-1+x)^3(-4442 + x(-15499 + x(-38722 + x(222115 +$

$11x(-42824 + 20203x)))) + k^5x^2(1427274 + x(-4230511 + 2x$

$(872810 + x(6586595 + x(-13525745 + (10584551 - 3015409x)x)))) -$

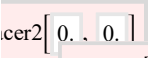

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In[161]:= k = 2;
a = 0.5;
a1 =  $\frac{(a^2 - 1)}{2}$ ; (*0.1,0.5,1,3*)
a2 = (a^2 - 1) a1;
We = 1;
x[1] = 0;
H = .643699;
For[ii = 1, ii ≤ 11, ii++,
  h = k - (k - 1) * x[ii];
  sol = NDSolve[{D[(u'[y] + We^2 a1 (u'[y])^3 + We^4 a2 (u'[y])^5), y, y] == 0, u[0] == 0,
    u'[0] == 1, u[h] == H, u'[h] == 0}, {u[y], u'[y], u''[y], u'''[y]}, {y, 0, h}];
  ppx = Table[(u^(3)[y] + 3 a1 We^2 u''[y]^2 u^(3)[y] + 5 a2 We^4 u''[y]^4 u^(3)[y]) /. sol,
    {y, 0, h, 0.1}];
  px[ii] = (u^(3)[y] + 3 a1 We^2 u''[y]^2 u^(3)[y] + 5 a2 We^4 u''[y]^4 u^(3)[y]) /. sol /. y → 0;
  x[ii + 1] = x[ii] + 0.1;
];
tt = Table[{x[ii], px[ii][[1]]}, {ii, 1, 11}];
fff = Interpolation[tt];
ggg = Integrate[Interpolation[tt][x], x];
hhh = Integrate[ggg, {x, 0, 1}];
Table[ggg, {x, 1, 1}]
(*pressure*)
Plot[ggg, {x, 0, 1}, Frame → True,
  PlotStyle → {{Thin, Black}}, LabelStyle → Directive[Black, 12],
  FrameLabel → {"", "", " ", ""}, FrameStyle → Directive[Thin],
  LabelStyle → Directive[18], Epilog → {Arrow[{{}}, {}], Text[""]}];
(*pressure gradient*)
Plot[fff[x], {x, 0, 1}, Frame → True, PlotRange → All,
  PlotStyle → {{Thick, Black}}, LabelStyle → Directive[Black, 12],
  FrameLabel → {"", "", " dp/px ", ""}, FrameStyle → Directive[Thin],
  LabelStyle → Directive[18], Epilog → {Arrow[{{}}, {}], Text[""]}];
(*velocity*)
Plot[u'[y] /. sol, {y, 0, h}, Frame → True,
  PlotStyle → {{Thick, Black}}, LabelStyle → Directive[Black, 12],
  FrameLabel → {"", "", " v ", ""}, FrameStyle → Directive[Thin],
  LabelStyle → Directive[18], Epilog → {Arrow[{{}}, {}], Text[""]}];

```

Out[173]= {0.0000486588}

```

In[9]:= u22 = 
   Spacer2[0.

```

```

In[1]:= a = 0.5;
η = 1;

```

$$\mu = 1;$$

$$k = 2; (*0.1, 0.2, 0.3*)$$

$$b = 1;$$

$$\alpha_1 = \frac{(a^2 - 1) \eta}{(\eta + \mu)}; (*0.1, 0.5, 1, 3*)$$

$$\alpha_2 = (a^2 - 1) \alpha_1;$$

$$pp = -\frac{6(-1+k)(-1+x)x}{(1+k)(k+x-kx)^2} -$$

$$\frac{1}{25k(1+k)^3(k+x-kx)^6} 12b^2(-1+k)(-1+x)x(k^3(79+k(-32+k(77+26k))) -$$

$$(-1+k)k^2(63+k(55+k(191+91k)))x + 3(-1+k)^2k(29+k(49+k(53+39k)))x^2 - (-1+k)^3(1+5k)(13+k(8+13k))x^3 + (-1+k)^4(13+k(8+13k))x^4) \alpha_1 +$$

$$\frac{1}{30625k^3(1+k)^5(k+x-kx)^{10}} 8b^4(-1+k)(-1+x)x$$

$$(9(-1+k)^2(26164k^{12}(-2+x)(-1+x)^7 + 26164x^7(1+x) + kx^6$$

$$(209312 + (26439 - 235201x)x) - k^{11}(-1+x)^6(-550 + x(-443963 + 235201x)) +$$

$$2k^{10}(-1+x)^5(-10945 + x(75985 + x(-906523 + 487927x))) +$$

$$2k^2x^5(353556 + x(-273280 + x(-557258 + 487927x))) + 4k^6(-1+x)x$$

$$(-168418 + (-1+x)x(-476296 + (-1+x)x(346861 + 1655413(-1+x)x))) -$$

$$5k^3x^4(-282331 + x(438137 + x(341729 + x(-1035337 + 498297x)))) -$$

$$5k^9(-1+x)^4(-39505 + x(-8772 + x(225500 + x(-957851 + 498297x)))) + 20k^4$$

$$x^3(85379 + x(-199689 + x(-23569 + x(560189 + 11x(-58191 + 20203x)))) +$$

$$20k^8(-1+x)^3(-4442 + x(-15499 + x(-38722 + x(222115 +$$

$$11x(-42824 + 20203x)))) + k^5x^2(1427274 + x(-4230511 + 2x$$

$$(872810 + x(6586595 + x(-13525745 + (10584551 - 3015409x)x)))) -$$

$$k^7(-1+x)^2(-202367 + x(234941 + 2x(-92500 + x(-1979055 +$$

$$x(5834125 + x(-7507903 + 3015409x)))))) \alpha_1^2 - 250(2k^7(3616 +$$

$$k(-4429 + k(4302 + k(-3193 + k(2038 + k(1683 + k(-1031 + 689k)))))) -$$

$$(-1+k)k^6(17267 + k(-21021 + k(15543 + k(-6983 +$$

$$k(14973 + k(25929 + k(-16843 + 10335k)))))) x +$$

$$(-1+k)^2k^5(40814 + k(-38829 + k(11524 + k(44317 + k(9938 +$$

$$k(88291 + k(-59476 + 33761k)))))) x^2 -$$

$$(-1+k)^3k^4(46410 + k(-31846 + k(-1865 + k(138739 + k(-36884 +$$

$$k(173044 + 13k(-9125 + 4823k)))))) x^3 +$$

$$(-1+k)^4k^3(40306 + k(-994 + k(-37264 + k(190331 + k(-92344 +$$

$$5k(42550 + k(-29230 + 14469k)))))) x^4 -$$

$$(-1+k)^5k^2(19292 + k(11438 + k(-58254 + k(155082 + k(-97575 +$$

$$k(167361 + k(-113837 + 53053k)))))) x^5 +$$

$$(-1+k)^6k(5512 + k(11044 + k(-38486 + k(78060 + k(-56266 +$$

$$k(81919 + k(-54688 + 24115k)))))) x^6 - (-1+k)^7(1+9k)$$

$$(689 + k(-1720 + k(2714 + k(-2228 + k(2714 + k(-1720 + 689k)))))) x^7 +$$

$$(-1+k)^8(689 + k(-1720 + k(2714 + k(-2228 + k(2714 + k(-1720 + 689k))))))$$

$$x^8) \alpha_2);$$

Plot[pp, {x, 0, 1}, PlotStyle -> {Thickness[0.007], Dashing[.030], Black},
LabelStyle -> Directive[Black, 12]]

`ln[10]: u33 =`

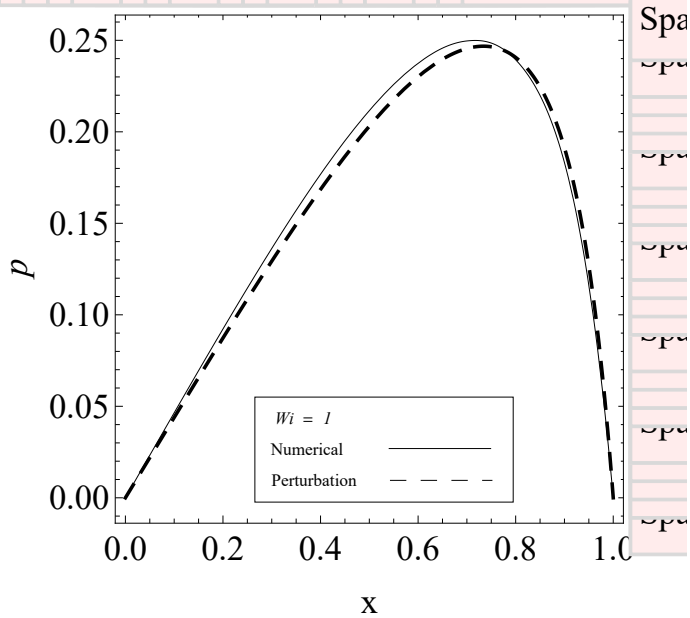


```
In[11]:= Show[{u22, u33}, Frame → True, PlotRange → All, LabelStyle → Directive[Black, 18],  
AspectRatio → 1, FrameLabel → {"x", "p", " a = 0.5, k = 2", ""},  
FrameStyle → Directive[Thin], LabelStyle → Directive[Black, 18], Axes → False]
```

```

  2  2  2 Sp  2  2 Sp  2  2 Sp  2  2 Sp  2  2 Spacer2| 0., 0.

```



```

In[108]:= k = 2;
a = 0.5;
η = 1;
μ = 1;

α1 =  $\frac{(a^2 - 1) \eta}{(\eta + \mu)}$ ; (*0.1,0.5,1,3*)
α2 =  $(a^2 - 1) \alpha_1$ ;
HHH =  $\frac{k}{1+k} +$ 
 $\left( b^2 \left( \frac{12 \alpha_1}{25 (1+k)^3} + \frac{156 \alpha_1}{25 k^3 (1+k)^3} - \frac{168 \alpha_1}{25 k^2 (1+k)^3} + \frac{12 \alpha_1}{25 k (1+k)^3} - \frac{168 k \alpha_1}{25 (1+k)^3} + \frac{156 k^2 \alpha_1}{25 (1+k)^3} \right) \right) /$ 
 $\left( -\frac{36}{(1+k)^3} - \frac{6}{k^2 (1+k)^3} - \frac{24}{k (1+k)^3} - \frac{24 k}{(1+k)^3} - \frac{6 k^2}{(1+k)^3} \right) +$ 
 $\left( b^4 \left( -\frac{2640312 \alpha_1^2}{30625 (1+k)^5} - \frac{1883808 \alpha_1^2}{30625 k^5 (1+k)^5} + \frac{3747816 \alpha_1^2}{30625 k^4 (1+k)^5} - \frac{126216 \alpha_1^2}{875 k^3 (1+k)^5} + \right.$ 
 $\frac{5193864 \alpha_1^2}{30625 k^2 (1+k)^5} - \frac{2640312 \alpha_1^2}{30625 k (1+k)^5} + \frac{5193864 k \alpha_1^2}{30625 (1+k)^5} - \frac{126216 k^2 \alpha_1^2}{875 (1+k)^5} +$ 
 $\frac{3747816 k^3 \alpha_1^2}{30625 (1+k)^5} - \frac{1883808 k^4 \alpha_1^2}{30625 (1+k)^5} + \frac{9344 \alpha_2}{245 (1+k)^5} + \frac{11024 \alpha_2}{245 k^5 (1+k)^5} -$ 
 $\frac{16496 \alpha_2}{245 k^4 (1+k)^5} + \frac{2272 \alpha_2}{35 k^3 (1+k)^5} - \frac{19776 \alpha_2}{245 k^2 (1+k)^5} + \frac{9344 \alpha_2}{245 k (1+k)^5} -$ 
 $\left. \frac{19776 k \alpha_2}{245 (1+k)^5} + \frac{2272 k^2 \alpha_2}{35 (1+k)^5} - \frac{16496 k^3 \alpha_2}{245 (1+k)^5} + \frac{11024 k^4 \alpha_2}{245 (1+k)^5} \right) \right) /$ 
 $\left( -\frac{90}{(1+k)^5} - \frac{6}{k^2 (1+k)^5} - \frac{36}{k (1+k)^5} - \frac{120 k}{(1+k)^5} - \frac{90 k^2}{(1+k)^5} - \frac{36 k^3}{(1+k)^5} - \frac{6 k^4}{(1+k)^5} \right)$ 
Plot[HHH, {b, 0, 0.5}, Frame → True, PlotRange → {0.666, .675},
PlotStyle → {{Thin, Black}}, LabelStyle → Directive[Black, 12],
FrameLabel → {"", "", " ", ""}, FrameStyle → Directive[Thin],
LabelStyle → Directive[18], Epilog → {Arrow[{{}}, {}], Text[""]}

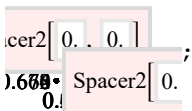
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Out[113]=  $\frac{2}{3} + 0.035 b^2 - 0.038774 b^4$ 

```

```

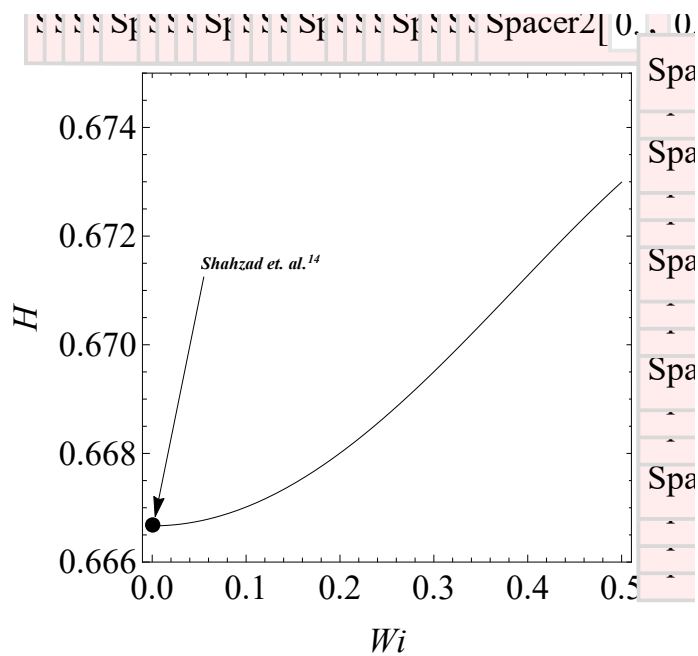
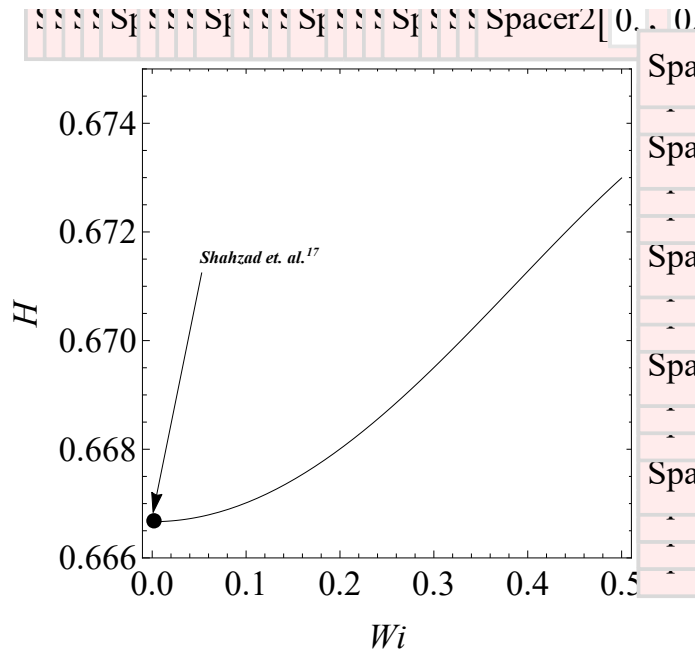
In[1]:= n1 = ;

```

```

In[2]:= Show[{n1}, Frame → True, PlotRange → {.666, .675}, LabelStyle → Directive[Black, 18],
AspectRatio → 1, FrameLabel → {"Wi", "H", " a = 0.5, k = 2", ""},
FrameStyle → Directive[Thin], LabelStyle → Directive[Black, 18], Axes → False]

```



```
In[15]:= a = 1;
η = 1;
μ = 1;
k = 6; (*2, 4, 6*)
x = 0.5;
α1 =  $\frac{(a^2 - 1) \eta}{(\eta + \mu)}$ ; (*0.1, 0.5, 1, 3*)
α2 =  $(a^2 - 1) \alpha_1$ ;
```

$$\begin{aligned}
pp = & -\frac{6(-1+k)(-1+x)x}{(1+k)(k+x-kx)^2} - \\
& \frac{1}{25k(1+k)^3(k+x-kx)^6} 12b^2(-1+k)(-1+x)x(k^3(79+k(-32+k(77+26k))) - \\
& (-1+k)k^2(63+k(55+k(191+91k)))x + 3(-1+k)^2k(29+k(49+k(53+39k))) \\
& x^2 - (-1+k)^3(1+5k)(13+k(8+13k))x^3 + (-1+k)^4(13+k(8+13k))x^4) \alpha_1 + \\
& \frac{1}{30625k^3(1+k)^5(k+x-kx)^{10}} 8b^4(-1+k)(-1+x)x \\
& (9(-1+k)^2(26164k^{12}(-2+x)(-1+x)^7 + 26164x^7(1+x) + kx^6 \\
& (209312 + (26439 - 235201x)x) - k^{11}(-1+x)^6(-550 + x(-443963 + 235201x)) + \\
& 2k^{10}(-1+x)^5(-10945 + x(75985 + x(-906523 + 487927x))) + \\
& 2k^2x^5(353556 + x(-273280 + x(-557258 + 487927x))) + 4k^6(-1+x)x \\
& (-168418 + (-1+x)x(-476296 + (-1+x)x(346861 + 1655413(-1+x)x))) - \\
& 5k^3x^4(-282331 + x(438137 + x(341729 + x(-1035337 + 498297x)))) - \\
& 5k^9(-1+x)^4(-39505 + x(-8772 + x(225500 + x(-957851 + 498297x)))) + 20k^4 \\
& x^3(85379 + x(-199689 + x(-23569 + x(560189 + 11x(-58191 + 20203x)))) + \\
& 20k^8(-1+x)^3(-4442 + x(-15499 + x(-38722 + x(222115 + \\
& 11x(-42824 + 20203x)))) + k^5x^2(1427274 + x(-4230511 + 2x \\
& (872810 + x(6586595 + x(-13525745 + (10584551 - 3015409x)x)))) - \\
& k^7(-1+x)^2(-202367 + x(234941 + 2x(-92500 + x(-1979055 + \\
& x(5834125 + x(-7507903 + 3015409x)))))) \alpha_1^2 - 250(2k^7(3616 + \\
& k(-4429 + k(4302 + k(-3193 + k(2038 + k(1683 + k(-1031 + 689k)))))) - \\
& (-1+k)k^6(17267 + k(-21021 + k(15543 + k(-6983 + \\
& k(14973 + k(25929 + k(-16843 + 10335k)))))) x + \\
& (-1+k)^2k^5(40814 + k(-38829 + k(11524 + k(44317 + k(9938 + \\
& k(88291 + k(-59476 + 33761k)))))) x^2 - \\
& (-1+k)^3k^4(46410 + k(-31846 + k(-1865 + k(138739 + k(-36884 + \\
& k(173044 + 13k(-9125 + 4823k)))))) x^3 + \\
& (-1+k)^4k^3(40306 + k(-994 + k(-37264 + k(190331 + k(-92344 + \\
& 5k(42550 + k(-29230 + 14469k)))))) x^4 - \\
& (-1+k)^5k^2(19292 + k(11438 + k(-58254 + k(155082 + k(-97575 + \\
& k(167361 + k(-113837 + 53053k)))))) x^5 + \\
& (-1+k)^6k(5512 + k(11044 + k(-38486 + k(78060 + k(-56266 + \\
& k(81919 + k(-54688 + 24115k)))))) x^6 - (-1+k)^7(1+9k) \\
& (689 + k(-1720 + k(2714 + k(-2228 + k(2714 + k(-1720 + 689k)))))) x^7 + \\
& (-1+k)^8(689 + k(-1720 + k(2714 + k(-2228 + k(2714 + k(-1720 + 689k)))))) \\
& x^8) \alpha_2); \\
\text{Plot}[pp, \{b, 0, .2\}, \text{Frame} \rightarrow \text{True}, \text{PlotStyle} \rightarrow \{\{\text{Thick}, \text{Black}\}\}, \\
\text{LabelStyle} \rightarrow \text{Directive}[\text{Black}, 12], \text{FrameLabel} \rightarrow \{\text{"", "", " ", ""\}, \\
\text{FrameStyle} \rightarrow \text{Directive}[\text{Thin}], \text{LabelStyle} \rightarrow \text{Directive}[18], \\
\text{Epilog} \rightarrow \{\text{Arrow}[\{\{\}, \{\}\}], \text{Text}[\text{""}]\}
\end{aligned}$$

```
In[22]:= o3 = cer2[0., 0.];
          0.06 • Spacer2[0.];
```

```
In[23]:= o2 = cer2[0., 0.];
          0.06 • Spacer2[0.];
```

```
In[24]:= o1 = cer2[0., 0.];
          0.06 • Spacer2[0.];
```

```
In[35]:= Show[{o1, o2, o3}, Frame → True, PlotRange → {0, .3},
  LabelStyle → Directive[Black, 18], AspectRatio → 1,
  FrameLabel → {"x", "p", " a = 0.5, k = 2", ""},
  FrameStyle → Directive[Thin], LabelStyle → Directive[Black, 18], Axes → False]
```

$a = 0.5, k = 2$

