

encountered are the parabola  $y - x^2 = 0$ , the hyperbola  $x^2 - y^2 - 1 = 0$ , and the ellipse  $x^2/4 + y^2 - 1 = 0$ .

You will be assigned one of the following curves to study. For your assigned curve

- (a)  $H(x, y) = x^3 - xy^2 + 1$
- (b)  $H(x, y) = x^3 - 2y^2 + \frac{3}{2}$
- (c)  $H(x, y) = x^3 + y^2 - 2xy - 1$
- (d)  $H(x, y) = x^3 - x - y^2 + 1$
- (e)  $H(x, y) = x^3y - x - y^2 + 1$
- (f)  $H(x, y) = x^3y - x - xy^2 + 1$
- (g)  $H(x, y) = x^3 - y - x^2y^2 + 1$
- (h)  $H(x, y) = x^3y - x - x^2y^2 + 1$
- (i)  $H(x, y) = x^3y - x - x^2y^2 - y^2 + 1$
- (j)  $H(x, y) = x^2y + x^3 + xy^3 + y + 1$

do the following

- (i) Use the `implicitplot` command to plot the portion of the curve that lies in the rectangle  $[-4, 2] \times [-4, 5]$  (see Maple/Calculus Notes). Use a fine enough grid so that the curve appears smooth. In the same picture plot the circle  $x^2 + y^2 = 1$  and use the `fsolve` command to find all points of intersection of this circle with the assigned curve. Annotate your picture, identifying the respective curves.
- (ii) For  $h = -.5, 0, .5$ , use the `fsolve` command to find all solutions to  $H(1 + h, y) = 0$ . This will give one or more points  $(1 + h, y)$  on the curve. Plot the tangent lines at these points (with suitable length) and the curve itself (for  $x \in [0, 2]$ ) in the same picture. Use colors to distinguish the respective plots. Print out and annotate your picture.
- (iii) Define two 1-dimensional arrays `p[i]`, `c[i]`,  $i=1..10$ . Store your favorite 10 colors in the array `c` (such as `c[2]:=magenta`). Then use a `do` loop to store the plots of the curves  $H(x, y) - i/10 = 0$ , for  $i = 1, \dots, 10$ , in the array `p`, with `p[i]` in color `c[i]`. Display all the plots in the same picture. Annotate this picture to clearly exhibit which curve goes with which value of  $i$ .

8. **(Plane Curves: The Parametric Description)** If two functions  $f, g : [a, b] \rightarrow \mathbb{R}$  are given on some interval  $[a, b]$ , then a curve is given parametrically by the two equations:

$$\begin{aligned} x &= f(t) \\ y &= g(t). \end{aligned}$$